





Compressive Sensing Based Grant-Free Random Access for Massive MTC

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System Model



Proposed Scheme



Simulation Results

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- Massive machine-type communications (mMTC) are poised to provide ubiquitous and unprecedent connectivity for billions of Internet of Things (IoT) devices^[1-2].
- The mMTC have the following features [1-3]:
 - > uplink-dominated
 - \succ sporadic traffic
 - \blacktriangleright low rates and short package
- Challenges :
 - \blacktriangleright the current grant-based random access schemes suffer from the low access efficiency and high latency caused by the complicated handshake procedure^[3].
 - > due to the limited available spectrum, it is impossible to allocate orthogonal radio resources to all potential devices.

A promising alternative:

grant-free random access scheme using non-orthogonal radio resources



- In grant-free random access scheme, the devices can directly transmit data to the base station (BS) without complicated handshaking process ^[4-5].
- Since non-orthogonal radio resources are adopted, the joint activity and data detection (JADD) needs to be efficiently solved at the BS.
- Due to the inherent sparsity of sporadic traffic, the JADD can be formulated as a compressive sensing (CS) problem^[4-5].
- Our works:
 - We design a beacon-aided grant-free massive access scheme based on the orthogonal frequency division multiplexing (OFDM) systems for mMTC.
 - An orthogonal approximate message passing-multiple measurement vectors (OAMP-MMV) algorithm is developed for JADD, where the prior knowledge of discrete constellation symbol and the structured sparsity of MMV model are fully exploited for improved performance.











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System Model 💋

- A single-antenna BS serves *K* single-antenna IoT devices, where *K* can be very large but only K_a ($K_a \ll K$) devices are active in each OFDM symbol interval.
- At the BS, the received signal $\mathbf{y}_t \in \mathbb{C}^{M \times 1}$ during the *t*-th OFDM symbol can be written as

$$\mathbf{y}_{t} = \sum_{k=1}^{K} \mathbf{H}_{k} \mathbf{s}_{k} \alpha_{k,t} \mathbf{x}_{k,t} + \mathbf{w}_{t} = \mathbf{S} \mathbf{x}_{t} + \mathbf{w}_{t}, \qquad (1)$$

where

- > $\mathbf{H}_{k} = \operatorname{diag}\left(\left[h_{1,k}, h_{2,k}, \cdots, h_{M,k}\right]^{\mathrm{T}}\right) \in \mathbb{C}^{M \times M}$, $h_{m,k}$ is the *m*-th subchannel between the *k*-th device and BS, $\mathbf{s}_{k} \in \mathbb{C}^{M \times 1}$ is the unique spreading sequence for the *k*-th device,
- > $\alpha_{k,t}$ is the binary activity indicator that equals one when the *k*-th device is active and zero otherwise,
- ➢ for active devices, x_{k,t} comes from a modulation
 constellation set Ω = {a₁, a₂, ···, a_L},

> $\mathbf{w}_t \sim \mathcal{CN}(\mathbf{0}, \sigma^2 \mathbf{I})$ is the additive white Gaussian noise,

$$\succ \mathbf{S} = [\mathbf{H}_1 \mathbf{s}_1, \mathbf{H}_2 \mathbf{s}_2, \cdots, \mathbf{H}_K \mathbf{s}_K] \in \mathbb{C}^{M \times K}, \text{ and} \\ \mathbf{x}_t = [\alpha_{1,t} x_{1,t}, \alpha_{2,t} x_{2,t}, \cdots, \alpha_{K,t} x_{K,t}]^{\mathrm{T}} \in \mathbb{C}^{K \times 1}.$$











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System Model



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- A. Overall Framework
- First, the BS periodically broadcasts a beacon for facilitating the synchronization and channel estimation at the devices.
- Define the estimated channel $\hat{\mathbf{H}}_k$, we assume that $\mathbf{H}_k \hat{\mathbf{H}}_k^{-1} = \mathbf{I}$ for simplicity.
- By taking the pre-equalization at the devices, we have the equivalent sensing matrix

$$\tilde{\mathbf{S}} = \begin{bmatrix} \mathbf{H}_1 \hat{\mathbf{H}}_1^{-1} \mathbf{s}_1, \mathbf{H}_2 \hat{\mathbf{H}}_2^{-1} \mathbf{s}_2, \cdots, \mathbf{H}_K \hat{\mathbf{H}}_K^{-1} \mathbf{s}_K \end{bmatrix}$$
$$= \begin{bmatrix} \mathbf{s}_1, \mathbf{s}_2, \cdots, \mathbf{s}_K \end{bmatrix}.$$
(2)

• In our scheme, we adopt that partial DFT matrix as the equivalent sensing matrix \tilde{S} .



Fig. 2. For the proposed frame structure, the beacon is periodically broadcast by the BS, and the activity of devices remains unchanged in *T* OFDM symbols.



Proposed Scheme

A. Overall Framework



$$\mathbf{Y} = \tilde{\mathbf{S}}\mathbf{X} + \mathbf{W},$$

where

- $\mathbf{Y} = [\mathbf{y}_1, \mathbf{y}_2, \cdots, \mathbf{y}_T] \in \mathbb{C}^{M \times T},$ $\mathbf{X} = [\mathbf{x}_1, \mathbf{x}_2, \cdots, \mathbf{x}_T] \in \mathbb{C}^{K \times T}, \text{ and}$ $\mathbf{W} = [\mathbf{w}_1, \mathbf{w}_2, \cdots, \mathbf{w}_T].$
- We further assume that the activity of devices remains unchanged in *T* continuous OFDM symbols, i.e., supp {x₁} = supp {x₂} = ··· = supp {x_T},

where $supp\{\cdot\}$ denotes the set of non-zero elements in a vector.



Fig. 2. For the proposed frame structure, the beacon is periodically broadcast by the BS, and the activity of devices remains unchanged in *T* OFDM symbols.



(3)

Proposed Scheme 💋

B. OAMP-MMV Algorithm for JADD



- We extend the conventional OAMP^[6] algorithm to the OAMP-MMV algorithm to leverage the structured sparsity in (4).
- Assume the distribution of $x_{k,t}$ as

$$p(x_{k,t}) = (1 - \lambda_{k,t}) \delta(x_{k,t}) + \frac{\lambda_{k,t}}{L} \sum_{l=1}^{L} \delta(x_{k,t} - a_l),$$
(5)

where $\lambda_{k,t} \in [0,1]$ denotes the non-zero probability of $x_{k,t}$ and can be termed as the sparsity ratio.

• By combining the a priori distribution in (5) with additive Gaussian noise model in [6], we can derive the approximate posterior distribution of $x_{k,t}$ as

$$p(x_{k,t} | r_{k,t}) = (1 - \pi_{k,t}) \delta(x_{k,t}) + \pi_{k,t} \frac{\sum_{l=1}^{L} g_{k,t,l} \delta(x_{k,t} - a_l)}{\sum_{l=1}^{L} g_{k,t,l}}, \qquad (6)$$

where $\pi_{k,t}$ can be termed as the posterior sparsity ratio.



B. OAMP-MMV Algorithm for JADD
Similar to the conventional OAMP algorithm ^[6], the proposed OAMP-MMV

algorithm has two basic modules, linear estimation (LE) module and non-linear estimation (NLE) module. They are iteratively executed until convergence.

 The final output is the MMSE estimation obtained in the NLE module, which relies on the posterior distribution in (6).



Fig. 3. Block diagram of the proposed OAMP-MMV algorithm.





B. OAMP-MMV Algorithm for JADD The expectation maximization (EM) algorithm^[7] is employed to learn the unknown parameters $\boldsymbol{\theta} = \left\{ \sigma_t^2, \lambda_{k,t}, \forall k, t \right\}$. (9) $\lambda_{k,t}^{i+1} = \pi_{k,t}^i, \forall k, t,$ $\left(\sigma^{2}\right)_{t}^{i+1} = \frac{1}{M} \left[\left\| \mathbf{y}_{t} - \tilde{\mathbf{S}}\boldsymbol{\mu}_{t}^{i} \right\|_{2}^{2} + \frac{M}{K} \sum_{i=1}^{K} \gamma_{k,t}^{i} \right], \forall t. (10)$ Exploit sparsity structure The update rule of $\lambda_{k,t}$ in (9) is refined as $\lambda_{k,1}^{i+1} = \lambda_{k,2}^{i+1} = \dots = \lambda_{k,T}^{i+1} = \frac{1}{T} \sum_{i=1}^{T} \pi_{k,t}^{i}, \forall k.$ (11)

Algorithm 1: OAMP-MMV algorithm			
Input: Y, $\tilde{\mathbf{S}}$, I_{iter} . Output: $\{\hat{\mathbf{x}}_t\}_{t=1}^T, \pi^f$. 1: $\forall k, t$: Set iteration index <i>i</i> to 1. Initialize $\mathbf{u}_t^0 = 0_K$ and			
		$v_t^0 = 1$. $\lambda_{k,t}^0$ and $(\sigma^2)_t^0$ are initialized as [12].	
	2:	for $i = 1$ to I_{iter} do	
	3:	%LE Module:	
	4:	$\forall t: \mathbf{r}_t^i = \mathbf{u}_t^{i-1} + \frac{\kappa}{M} \mathbf{S}^{H} \left(\mathbf{y}_t - \mathbf{S} \mathbf{u}_t^{i-1} \right).$	
	5:	$\forall t: \tau_t^i = \frac{K - M}{M} v_t^{i-1} + \frac{K}{M} (\sigma^2)_t^{i-1}.$	
	6:	%NLE Module:	
	7:	$\forall k, t, l: g_{k,t,l}^{i} = \exp\left(-\frac{ a_{l} ^{2} - 2\Re\epsilon\{a_{l}^{+}r_{k,t}^{+}\}}{\tau_{t}^{i}}\right).$	
	8:	$\forall k, t: \pi_{k,t}^{i} = \left[1 + (1 - \lambda_{k,t}^{i-1}) / (\frac{\lambda_{k,t}^{i-1}}{L} \sum_{l=1}^{L} g_{k,t,l}^{i}) \right]^{-1}.$	
)	9:	$\forall k, t: \mu_{k,t}^{i} = (\pi_{k,t}^{i} \sum_{l=1}^{L} a_{l} g_{k,t,l}^{i}) / (\sum_{l=1}^{L} g_{k,t,l}^{i}).$	
	10:	$\forall k, t: \gamma_{k,t}^{i} = (\pi_{k,t}^{i} \sum_{l=1}^{L} a_{l} ^{2} g_{k,t,l}^{i}) / (\sum_{l=1}^{L} g_{k,t,l}^{i}) - \mu_{k,t}^{i} ^{2}.$	
	11:	$\forall t: \bar{\gamma}_t^i = \frac{1}{K} \sum_{k=1}^K \gamma_{k,t}^i, v_t^i = \left(\frac{1}{\bar{\gamma}_t^i} - \frac{1}{\tau_t^i}\right)^{-1}.$	
	12:	$\forall k, t: C_t^i = \frac{\tau_t^i}{\tau^{\frac{i}{2}} - \bar{\tau}^{\frac{i}{2}}}, \ u_{k,t}^i = C_t^i \left(\mu_{k,t}^i - \frac{\bar{\gamma}_t^i}{\tau^{\frac{i}{2}}} r_{k,t}^i \right).$	
	13:	%EM Update:	
	14:	$\forall t$: Update $(\sigma^2)_t^i$ using (10).	
	15:	$\forall k, t$: Update $\lambda_{k,t}^i$ using (11).	
	16:	end for	
	17:	$orall t: \hat{oldsymbol{x}}_t = oldsymbol{\mu}_t^i, oldsymbol{\pi}^f = oldsymbol{\lambda}^i.$	





B. OAMP-MMV Algorithm for JADD

• To identify active devices, a hard threshold based activity detector is developed as follows

$$\hat{\alpha}_{k} = \begin{cases} 1, & \pi_{k}^{f} \ge T_{h} \\ 0, & \text{otherwise} \end{cases}, \forall k, \qquad (12)$$

where $\hat{\alpha}_k = 1$ indicates that the *k*-th device is active, and T_h is a threshold which is determined empirically. Algorithm 1: OAMP-MMV algorithm $\mathbf{Y}, \, \mathbf{\tilde{S}}, \, I_{\text{iter}}.$ Input: **Output:** $\{\hat{x}_t\}_{t=1}^T, \pi^f$. 1: $\forall k, t$: Set iteration index *i* to 1. Initialize $\mathbf{u}_t^0 = \mathbf{0}_K$ and $v_t^0 = 1$. $\lambda_{k,t}^0$ and $(\sigma^2)_t^0$ are initialized as [12]. 2: for i = 1 to I_{iter} do %LE Module: 3: $\forall t: \mathbf{r}_t^i = \mathbf{u}_t^{i-1} + \frac{K}{M} \mathbf{\tilde{S}}^{\mathrm{H}} \left(\mathbf{y}_t - \mathbf{\tilde{S}} \mathbf{u}_t^{i-1} \right).$ 4: $\forall t: \tau_t^i = \frac{K-M}{M} v_t^{i-1} + \frac{\dot{K}}{M} (\sigma^2)_t^{i-1}.$ 5: 6: %NLE Module: $\forall k, t, l: g_{k,t,l}^{i} = \exp\left(-\frac{|a_{l}|^{2} - 2\Re \mathfrak{e}\left\{a_{l}^{*} r_{k,t}^{i}\right\}}{\tau_{*}^{i}}\right).$ 7: $\forall k, t: \pi_{k,t}^{i} = \left[1 + (1 - \lambda_{k,t}^{i-1}) / (\frac{\lambda_{k,t}^{i-1}}{L} \sum_{l=1}^{L} g_{k,t,l}^{i}) \right]^{-1}.$ 8: $\forall k, t: \mu_{k,t}^i = (\pi_{k,t}^i \sum_{l=1}^L a_l g_{k,t,l}^i) / (\sum_{l=1}^L g_{k,t,l}^i).$ 9: $\forall k, t: \gamma_{k,t}^i = (\pi_{k,t}^i \sum_{l=1}^L |a_l|^2 g_{k,t,l}^i) / (\sum_{l=1}^L g_{k,t,l}^i) - |\mu_{k,t}^i|^2.$ 10: $\forall t: \, \bar{\gamma}_t^i = \frac{1}{K} \, \sum_{i=1}^K \, \gamma_{k,t}^i, \, v_t^i = \left(\frac{1}{\bar{\gamma}_t^i} - \frac{1}{\tau_t^i}\right)^{-1}.$ 11: $\forall k, t: C_t^i = \frac{\tau_t^i}{\tau_t^i - \bar{\gamma}_t^i}, \ u_{k,t}^i = C_t^i \left(\mu_{k,t}^i - \frac{\bar{\gamma}_t^i}{\tau_t^i} r_{k,t}^i \right).$ 12: %EM Update: 13: $\forall t$: Update $(\sigma^2)_t^i$ using (10). 14: $\forall k, t$: Update $\lambda_{k,t}^i$ using (11). 15: 16: end for 17: $\forall t: \hat{\boldsymbol{x}}_t = \boldsymbol{\mu}_t^i, \, \boldsymbol{\pi}^f = \boldsymbol{\lambda}^i.$











System Model



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Proposed Scheme

Simulation Results

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• Simulation Parameters

The number of potential IoT devices K	500
The number of active devices K_a	50
The number of measurements M	70
Modulation	QPSK
The threshold of activity detector T_h	1/3
The number of iterations	30

• We define the error detection probability of activity detection (P_e) and BER as follows

$$P_{e} = \frac{1}{K} \sum_{k=1}^{K} |\hat{\alpha}_{k} - \alpha_{k}|, \qquad \text{BER} = 1 - \frac{N_{s}}{K_{a} T \log_{2} L}, \qquad (13)$$

where N_s denotes the number of correctly decoded bits of successfully detected devices.



Fig. 4. Comparison of the different detection algorithms versus SNR with T = 10: (a) P_e ; (b) BER.

Our proposed OAMP-MMV algorithm achieves superior performance over the baseline algorithms!

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Fig. 5. Comparison of the different detection algorithms versus *T* continuous OFDM symbols with SNR = 10 dB: (a) P_e ; (b) BER.

Our proposed OAMP-MMV algorithm outperforms the baseline algorithms!

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Thanks for your listening!



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