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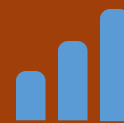
# Joint Channel Estimation and Radar Sensing for UAV Networks with mmWave Massive MIMO

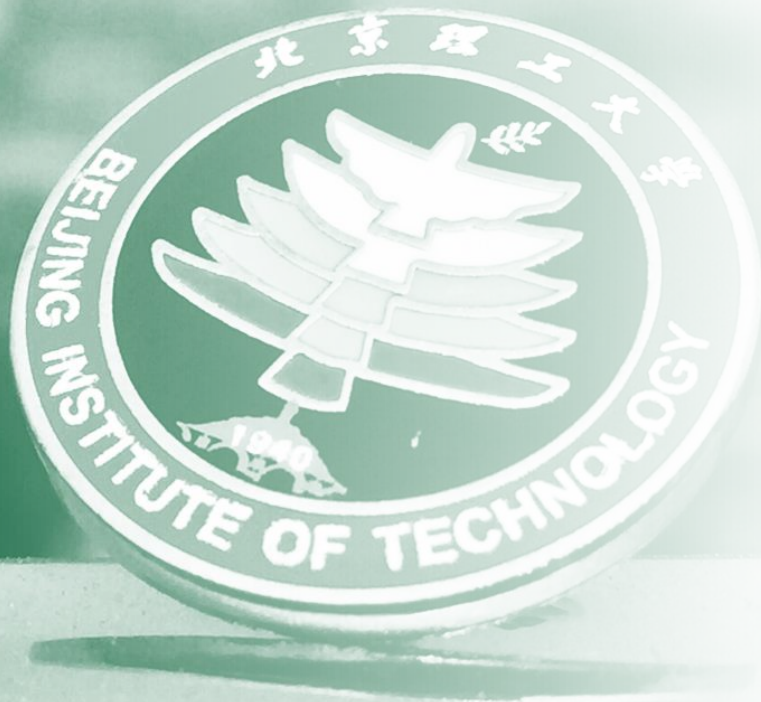
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## 1 Introduction

## 2 System and Channel Models

## 3 Proposed ISAC Architecture



- A. Full-Duplex and SI Cancellation
- B. Waveform Design

## 4 Proposed CS-based Solution

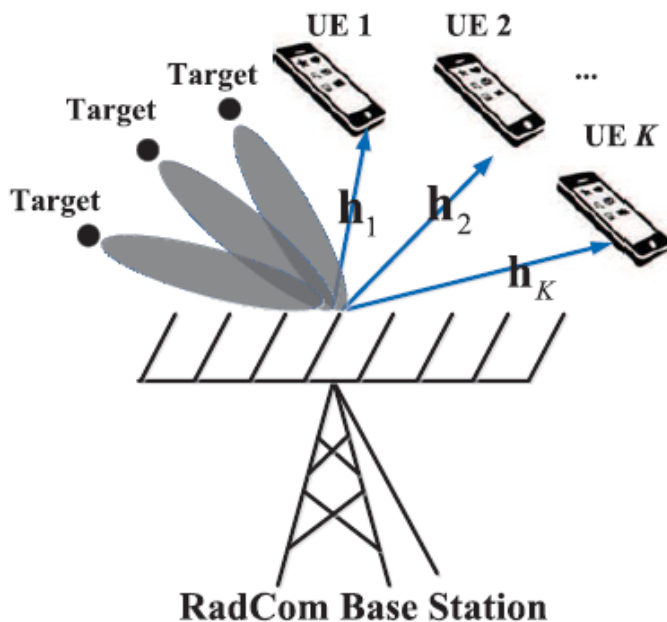
- A. Dictionary Design
- B. Proposed CS-based Algorithms

## 5 Simulation Results

## 6 Future Works



- **Integrated Sensing and Communication (ISAC)** [R1]-[R2]
  - Integrate both functionalities of radar and communications, saving spectrum and hardware resources.
- **Unmanned Aerial Vehicle (UAV) Networks** [R3]
  - Play an important role in the non-terrestrial network (NTN)
  - Flexible deployment, fast response, line-of-sight (LoS) transmission, etc.
- It will be exciting to combine **ISAC** with **UAV** networks [R4].
- The state-of-the-art **compressive sensing (CS)** is applied to facilitate **joint channel estimation (CE)** and radar sensing.





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- A ground-to-air (G2A) ISAC scenario in UAV networks.
- At the terrestrial station, the full duplex (FD) [R5]-[R6] mmWave massive MIMO with hybrid beamforming (HBF) is deployed.

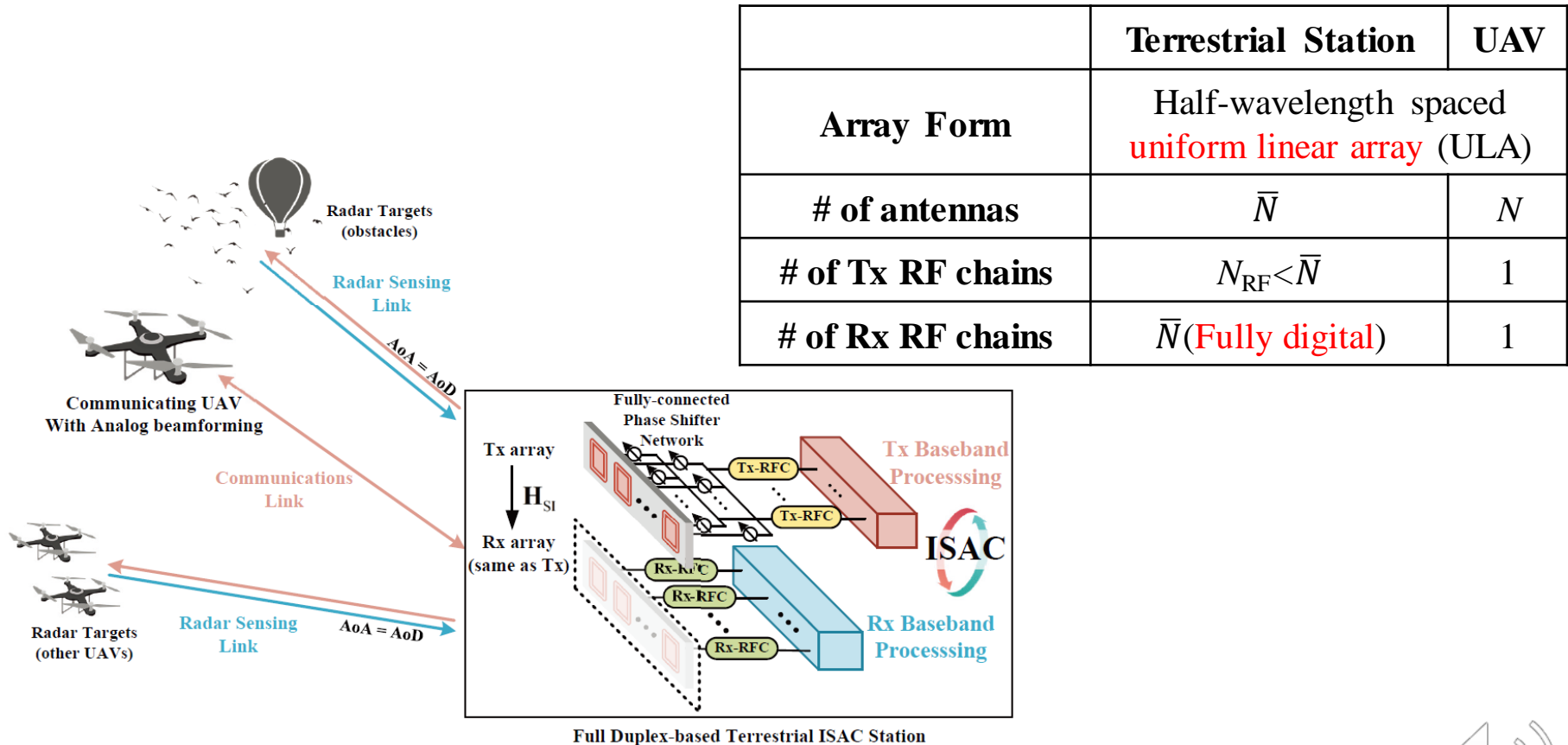


Fig. 1. The model of the considered UAV network, where the terrestrial ISAC station with FD mmWave mMIMO serves UAVs.





- The delay-domain **communication channel** with one LoS path and  $N_C$  NLoS clusters:

Pulse shaping filter  
with delay offset

$$\mathbf{H}(\tau) = \mathbf{H}_{\text{LoS}} p(\tau - \tau_{\text{LoS}}) + \sum_{c=1}^{N_C} \sum_{l=1}^{N_P} \mathbf{H}_{c,l} p(\tau - \tau_{c,l}), \quad (1)$$

with

$$\mathbf{H}_{\text{LoS}} = \sqrt{N\bar{N}} g_{\text{LoS}} \mathbf{a}_N(\theta_{\text{LoS}}) \mathbf{a}_N^H(\varphi_{\text{LoS}}), \quad (2)$$

Steering vectors  
with AoA and AoD

$$\mathbf{H}_{c,l} = \sqrt{\frac{N\bar{N}}{K_f N_C N_P}} g_{c,l} \mathbf{a}_N(\theta_{c,l}) \mathbf{a}_N^H(\varphi_{c,l}). \quad (3)$$

- The delay-domain **radar channel** (from the station to the targets and then back to station) with **spatial consistency** [Journal].

$$\bar{\mathbf{H}}(\tau) = \sum_{c=1}^{\bar{N}_C} \sum_{l=1}^{\bar{N}_P} \bar{\mathbf{H}}_{c,l} p(\tau - \bar{\tau}_{c,l}), \quad (5)$$

where

$$\bar{\mathbf{H}}_{c,l} = \sqrt{\frac{\bar{N}^2}{\bar{N}_C \bar{N}_P}} \bar{g}_{c,l} \mathbf{a}_{\bar{N}}(\bar{\theta}_{c,l}) \mathbf{a}_{\bar{N}}^H(\bar{\theta}_{c,l}). \quad (6)$$

Spatial Consistency,  
i.e., AoA=AoD for  
radar sensing

[Journal] Z. Gao, Z. Wan *et al.*, “Integrated Sensing and Communication with mmWave Massive MIMO: A Compressed Sampling Perspective”, submitted to *IEEE TWC*, Major Revision. arXiv: 2201.05766



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# 3.A Full-duplex and SI Cancellation



- To conduct the joint CE and radar sensing, the terrestrial station transmits the known pilot signals  $\mathbf{p}_p \in \mathbb{C}^{N \times 1}$  with  $\|\mathbf{p}_p\|_2 = P_{Tx}$ .
- At the Rx part of terrestrial station, the received signals after reflection:

$$\bar{\mathbf{Y}} = \bar{\mathbf{H}}_{SD} \bar{\Phi} + \bar{\mathbf{H}}_{SI} \bar{\mathbf{P}} + \bar{\mathbf{N}}, \quad (8)$$

Received echo signals      Self-interference (SI)      AWGN

where  $\bar{\mathbf{H}}_{SD} \in \mathbb{C}^{\bar{N} \times L\bar{N}}$  is the effective radar CIR to be estimated, containing the information of delays (ranges) and angles of targets.

- At the UAV, the analog beamformer weight vectors  $\mathbf{w}_q \in \mathbb{C}^{M \times 1}$ ,  $q = 0, 1, \dots, Q - 1$  are used to receive the downlink pilot signals from terrestrial station. The received signals:

$$\mathbf{y} = \Phi \text{vec}(\mathbf{H}_{SD}) + \mathbf{n}, \quad (10)$$

where  $\Phi$  is the known measurement matrix (consisting of pilot signals), and  $\mathbf{H}_{SD}$  is the effective communications CIR to be estimated.



- (8) and (10) are usually under-determined, which motivates us to resort to CS techniques.



# 3.A Full-duplex and SI Cancellation

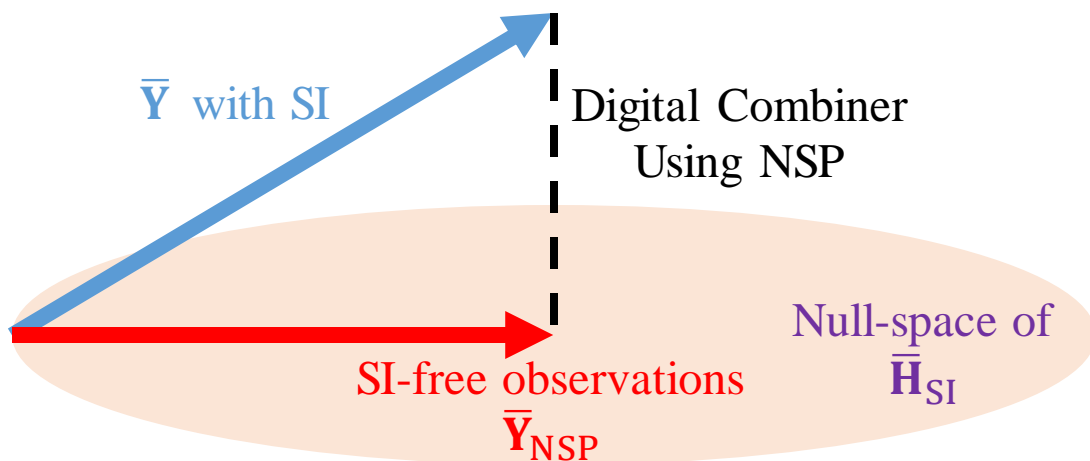


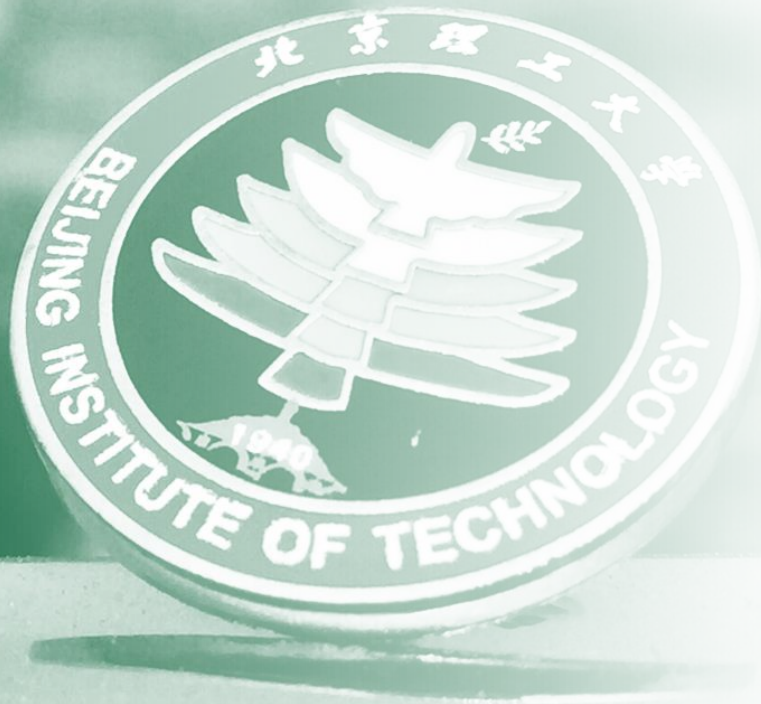
- Assume the SI channel  $\bar{\mathbf{H}}_{\text{SI}}$  is known [R5]-[R6]
- Since the same array are used for both Tx and Rx, the SI channel will be highly-correlated so that it will be rank-insufficient.
- We apply a digital combiner  $\bar{\mathbf{W}} \in \mathbb{C}^{\bar{N} \times \bar{N}}$  to the receive signals  $\bar{\mathbf{Y}}$  following the null-space projection (NSP) method [R6]:

$$\bar{\mathbf{W}} = \mathbf{I}_{\bar{N}} - \bar{\mathbf{H}}_{\text{SI}} \bar{\mathbf{P}} (\bar{\mathbf{H}}_{\text{SI}} \bar{\mathbf{P}})^{\dagger}. \quad (13)$$

- The SI-free received signals for radar sensing:

$$\bar{\mathbf{Y}}_{\text{NSP}} \triangleq \bar{\mathbf{W}} \bar{\mathbf{Y}} = \bar{\mathbf{W}} \bar{\mathbf{H}}_{\text{SD}} \bar{\Phi} + \bar{\mathbf{W}} \bar{\mathbf{N}} \quad (14)$$





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# 3.B Waveform Design



- We note that in HBF architecture, the switch of phase shifter will take non-negligible reconfiguring time [R7], while this property is often sidestepped in previous works [R2] on waveform design.
- Given that, we propose to use a **codebook** of analog precoders (combiners) and to reserve **sufficient idle time for reconfiguring RF circuits** between two adjacent codewords, at the cost of loss of **pilot diversity**.

$$\text{Analog Precoder Codebook} \\ \left\{ \mathbf{F}_n^{\text{CB}} \in \mathbb{C}^{\bar{N} \times N_{\text{RF}}} \right\}_{n=1}^{\bar{N}^{\text{CB}}}$$



$$\text{Analog Combiner Codebook} \\ \left\{ \mathbf{w}_n^{\text{CB}} \in \mathbb{C}^{N \times 1} \right\}_{n=1}^{N^{\text{CB}}}$$

**Only  $\bar{N}^{\text{CB}}$  ( $N^{\text{CB}}$ ) codewords are allocated to  $P$  ( $Q$ ) pilot signals, reducing pilot diversity**

Reconfiguring.....

$$\mathbf{F}_p = \begin{cases} \mathbf{F}_{\lceil (p+1)/\bar{T}_{\text{RF}} \rceil}^{\text{CB}}, & \text{mod}(p, \bar{T}_{\text{RF}}) < \bar{T}_{\text{RF}} - T_{\text{GI}}, \\ \text{uncertain,} & \text{otherwise,} \end{cases} \quad (16)$$

$$\mathbf{w}_n = \begin{cases} \mathbf{w}_{\lceil (n+1)/T_{\text{RF}} \rceil}^{\text{CB}}, & \text{mod}(n, T_{\text{RF}}) < T_{\text{RF}} - T_{\text{GI}}, \\ \text{uncertain,} & \text{otherwise.} \end{cases} \quad (17)$$

# 3.B Waveform Design

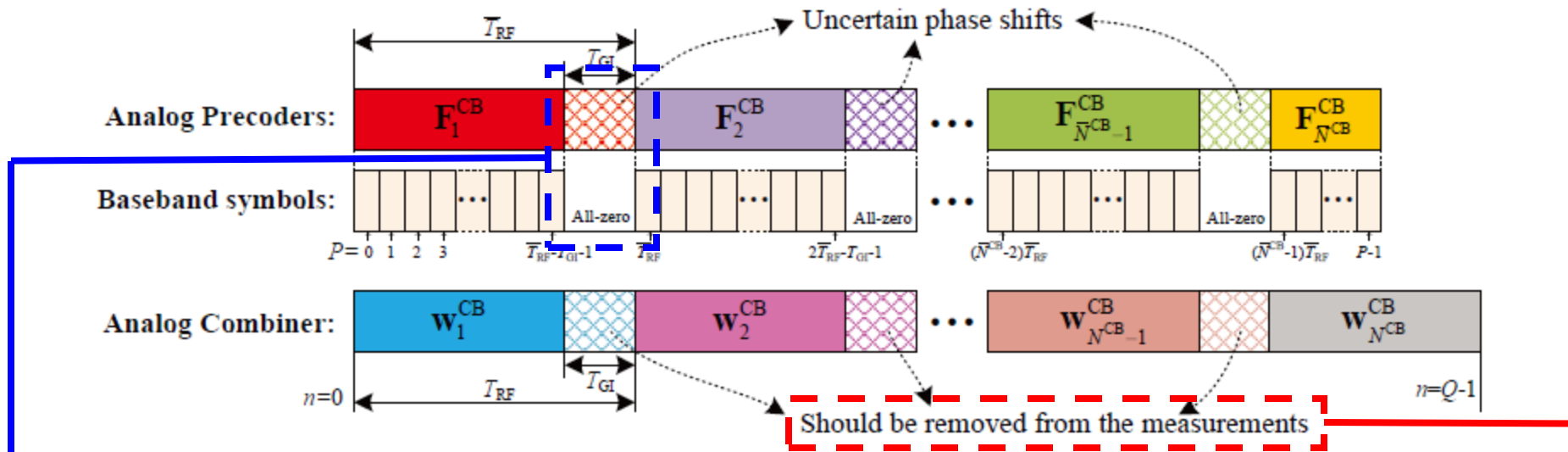


Fig. 2. The proposed waveform design which considers both the pilot diversity and the hardware feasibility.

- During the stage of uncertain analog precoders, zero baseband signals are transmitted, i.e., the actual transmit signals are also zeros:

$$s_p = \mathbf{0}_{N_{RF} \times 1} \text{ when } \text{mod}(p, \bar{T}_{RF}) \geq \bar{T}_{RF} - T_{GI}. \quad (18)$$

- For the uncertain analog combiners, we remove them from the valid measurements:

$$\mathbf{y}_v = \Phi_v \text{vec}(\mathbf{H}_{SD}) + \mathbf{n}_v, \quad (19)$$

where  $\mathbf{y}_v = [\mathbf{y}]_{\mathcal{I}_v}$ ,  $\mathbf{n}_v = [\mathbf{n}]_{\mathcal{I}_v}$ ,  $\Phi_v = [\Phi]_{\mathcal{I}_v}$ , and the ordered set for valid measurements  $\mathcal{I}_{\text{valid}} = \{i + 1 \mid 0 \leq i < Q, \text{mod}(i, T_{RF}) < T_{RF} - T_{GI}\}$ .





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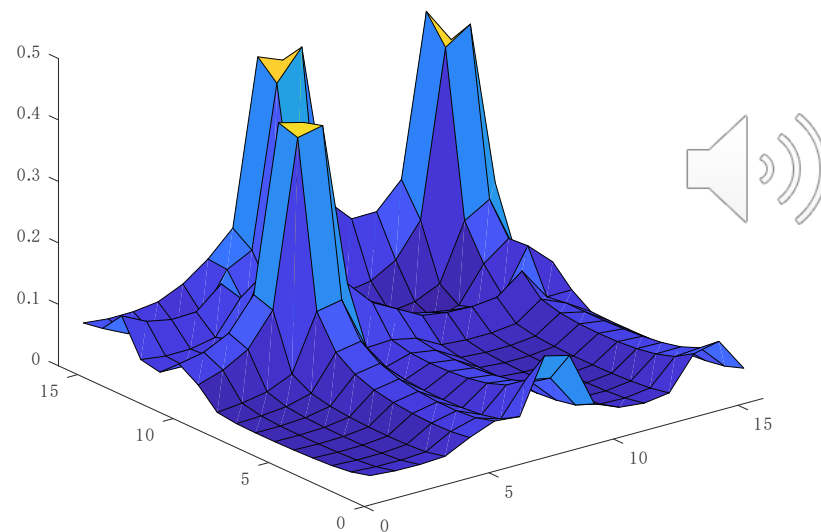
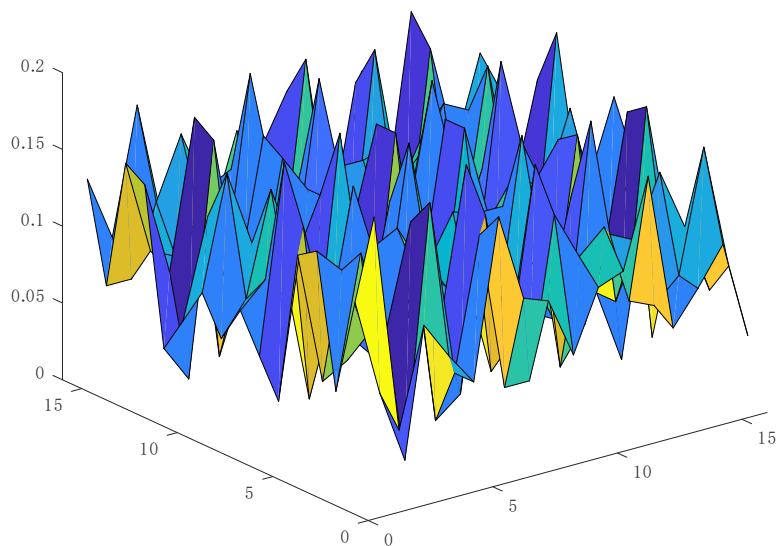
# 4.A Dictionary Design



- **Compressive sensing** [R7]-[R8]: leveraging the **sparsity** of mmWave channels in many aspects to significantly reduce the pilot overhead in channel estimation and radar sensing.
- Re-represent the channels with the dictionaries  $\mathbf{A}_T \in \mathbb{C}^{\bar{N} \times G_T}$ ,  $\mathbf{A}_R \in \mathbb{C}^{\bar{N} \times G_R}$  and  $\mathbf{A} \in \mathbb{C}^{N \times G}$

$$\overline{\mathbf{H}}_l \approx \mathbf{A}_R \overline{\mathbf{H}}_l^{\text{Ad}} \mathbf{A}_T^H, \quad (20)$$

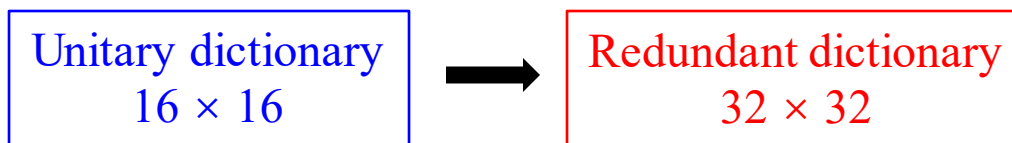
$$\mathbf{H}_l \approx \mathbf{A} \mathbf{H}_l^{\text{Ad}} \mathbf{A}_T^H, \quad (21)$$



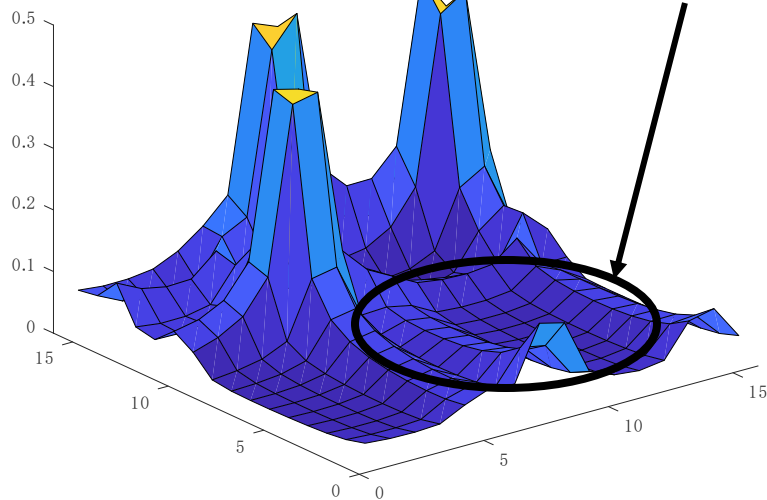
# 4.A Dictionary Design



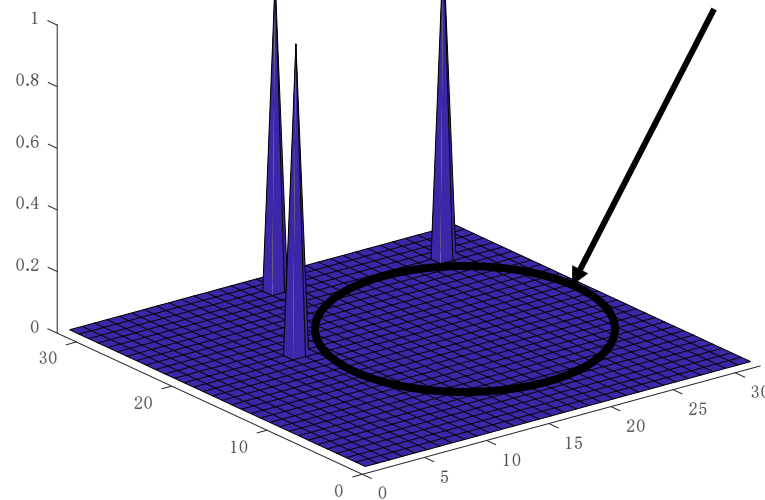
- Redundant dictionary [R8]: trading off the complexity and estimation performance.



The power leakage that degrades the sparsity.



Larger dimension, enhanced sparsity



- Given the spatial consistency, i.e.,  $\text{AoA}=\text{AoD}$  in radar sensing, we use multi-resolution (MR) dictionary design for radar sensing.
- Unitary dictionary for the Tx part, while redundant dictionary for the Rx part.





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# 4.B Proposed CS-based Algorithms



- Multi-resolution Orthogonal Matching Pursuit (MR-OMP) to recover the radar CIR:

**Algorithm 1** Mixed-resolution Orthogonal Matching Pursuit (MR-OMP)

**Input:**  $\bar{\mathbf{Y}}_{\text{NSP}}$ ,  $\bar{\Phi}$ ,  $\bar{\mathbf{W}}$ ,  $\mathbf{A}_T$ ,  $\mathbf{A}_R$ , and *stop criterion*.

1: **Initialization:**  $\Psi = \left[ \bar{\Phi}^T (\mathbf{I}_L \otimes \mathbf{A}_T^*) \right] \otimes (\bar{\mathbf{W}} \mathbf{A}_R)$ ,  $\mathbf{r} = \text{vec}(\bar{\mathbf{Y}}_{\text{NSP}})$ , and  $\mathcal{I} = \mathcal{I}_D = \mathcal{I}_A = \emptyset$ .

2: **while** *stop criterion* is not met, **do**

3:  $i_{\max} = \arg \max_i |[\Psi^H \mathbf{r}]_i|$ ;

4:  $\mathcal{I} = \mathcal{I} \cup \{i_{\max}\}$ ;

5: Based on  $i_{\max}$ , obtain the delay estimate  $\hat{\tau}$  and the angle estimate  $\hat{\theta}$  at the Rx part;

6:  $\mathcal{I}_D = \mathcal{I}_D \cup \{\hat{\tau}\}$ ; % Delay Estimation.

7:  $\mathcal{I}_A = \mathcal{I}_A \cup \{\hat{\theta}\}$ ; % Angle Estimation.

8:  $\Phi_{\text{aux}} = \left[ \bar{\Phi}^T \otimes \bar{\mathbf{W}} \right]_{\{(i_d-1)\bar{N}+1:i_d\bar{N}\}}$  where  $i_d$  is the integer closest to  $\frac{\hat{\tau}}{T_s} + 1$ , and  $\mathbf{a}_{\text{aux}} = \bar{\mathbf{a}}_{\bar{N}}(\hat{\theta})$ ;

9: Replace  $[\Psi]_{\{i_{\max}\}}$  by  $\mathbf{q} = (\Phi_{\text{aux}} \mathbf{a}_{\text{aux}}^*) \otimes \mathbf{a}_{\text{aux}}$ ;

10:  $\hat{\mathbf{g}} = [\Psi]_{\mathcal{I}}^\dagger \text{vec}(\bar{\mathbf{Y}}_{\text{NSP}})$ ;

11:  $\mathbf{r} = \text{vec}(\bar{\mathbf{Y}}_{\text{NSP}}) - [\Psi]_{\mathcal{I}} \hat{\mathbf{g}}$ ;

12: **end while**

13: Reconstruct estimate  $\hat{\bar{\mathbf{H}}}_{\text{SD}}$  of  $\bar{\mathbf{H}}_{\text{SD}}$  via (5)-(7) based on  $\mathcal{I}_D$ ,  $\mathcal{I}_A$ , and  $\hat{\mathbf{g}}$ ;

**Output:** Estimate  $\hat{\bar{\mathbf{H}}}_{\text{SD}}$  of  $\bar{\mathbf{H}}_{\text{SD}}$ , estimated target delays  $\mathcal{I}_D$ , and estimated target angles  $\mathcal{I}_A$ .

An extension of OMP algorithm considering the spatial consistency and the MR dictionaries

The measurement matrix will be refined by replacing the lower-resolution angle estimate at the Tx part by the higher-resolution angle estimate at the Rx part



# 4.B CS-based ISAC Solutions



- Low-complexity CE scheme for energy-constraint UAVs to recover the LoS component of communication channels:

$$i_{\text{LoS}} = \arg \max_i | [((\mathbf{I}_L \otimes \mathbf{A}_T^T) \otimes \mathbf{A}^H) \Phi_v^H \mathbf{y}_v]_i |, \quad (24)$$

A single correlation step of the OMP framework

The estimate of LoS component will be fed back to the terrestrial station to conduct beamforming for payload data transmission.





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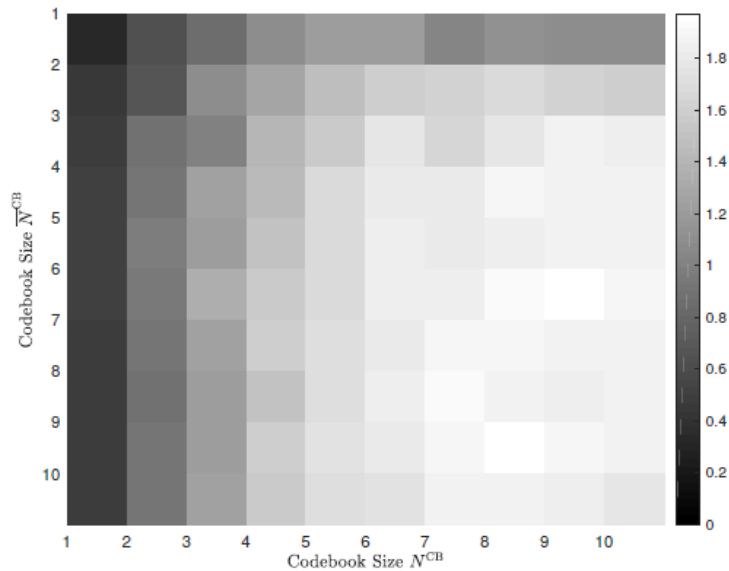
## 6 Future Works



### Simulation Parameters

- Carrier frequency 77 GHz ( $\lambda=3.9$  mm)
- $\bar{N} = 16, N = 8, N_{\text{RF}} = 4$
- $\bar{N}_{\text{C}} = N_{\text{C}} = 6, \bar{N}_{\text{P}} = N_{\text{P}} = 15$
- The maximum path-delay is  $LT_{\text{S}}$  with  $L=32$  and sampling period  $T_{\text{S}}=5$  ns

The average spectral efficiency (ASE) performance v.s. the sizes of codebooks for waveform design



- ◆ Small size of codebook brings poor ASE performance due to the lack of pilot diversity
- ◆ Choosing appropriate codebook size trades off the system performance and storage burden

Fig. 3. Phase transition in ASE performance versus the codebook sizes  $\bar{N}^{\text{CB}}$  and  $N^{\text{CB}}$ .





### Simulation Parameters

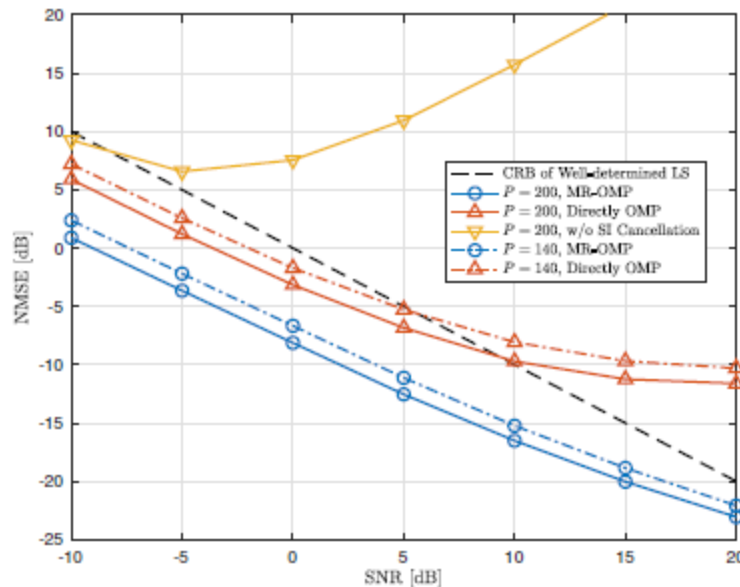
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- The maximum path-delay is  $LT_S$  with  $L=32$  and sampling period  $T_S=5$  ns

**Benchmark 1:** Cramér-Rao bound (CRB) of Well-determined LS;

**Benchmark 2:** Original OMP algorithm<sup>[R8]</sup> ignoring spatial consistency

**Benchmark 3:** The proposed MR-OMP algorithm **without SI cancellation**

The normalized mean-square-error (NMSE) performance v.s. signal-to-noise ratio (SNR)



◆ It indicates the necessity of SI cancellation for FD ISAC systems.

◆ The proposed MR-OMP outperforms the benchmarks significantly.

Fig. 4. Performance comparison of different radar CIR recovery algorithms. The impact of SI is also presented.





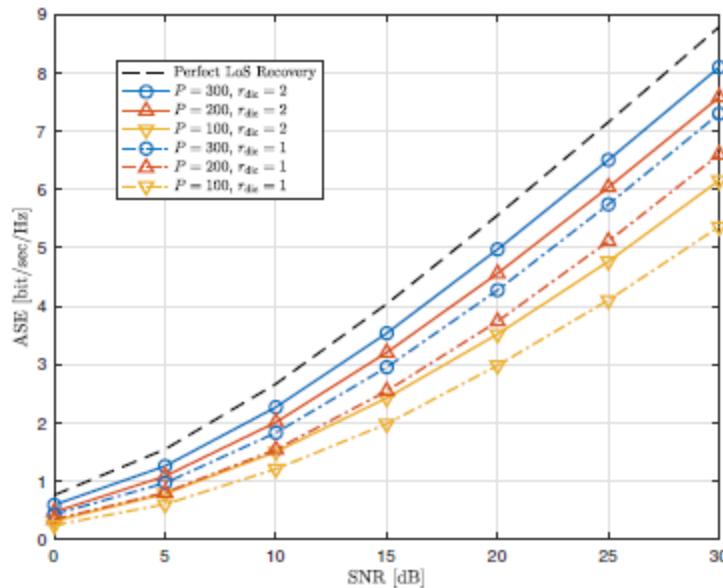
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**Benchmark 1: Perfect LoS recovery**

**Benchmark 2: Unitary dictionary for channel estimation**

### The average spectral efficiency (ASE) performance v.s. signal-to-noise ratio (SNR)



◆ The performance of the proposed low-complexity CE scheme can approach that of the perfect channel recovery

◆ Redundant dictionary can effectively improve the performance

Fig. 5. ASE performance versus SNR. Different values of  $P$  and  $r_{\text{dic}}$  are considered.





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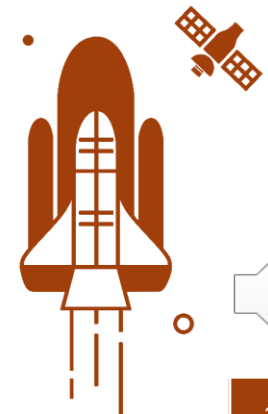
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Thanks for your listening

Any questions are welcome



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